ABBA Linear Ball Rail ---- $B R$ series

## International Standard Dimension Design

## Characteristics of ABBA Linear Ball Rail



Smooth running due to new ball re-circulation (patent)

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## Comparison of ABBA 4-row circular arc and 2-row Gothic arch



## Comparison :

1. Light motion : The circular arc design has the smaller differential slip than Gothic arch.
2. Low installation accuracy : The circular arc design can achieve the ideal two-point contact structure. When balls occur elastic deformation at the contact points, the circular arc design has the better ability of absorbing errors on the installation surfaces without compromising smooth, light motion.
3. Low frictional resistance : Due to the two-point contact structure for the circular arc design, even when we preload to the intended rigidity, the friction will not significantly increase.
4. High load rating : The radius of curvature of the ball rolling track for the circular arc design is $\mathbf{5 2}$ to $\mathbf{5 3 \%}$ of the ball diameter and the Gothic arch is 55 to $\mathbf{6 0 \%}$.

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Unit : mm

| ITEM GRADE | $\begin{array}{\|c\|} \hline \text { Normal } \\ (\mathbf{N}) \end{array}$ | High ( H ) | Precision <br> ( P ) | $\begin{array}{\|c} \hline \text { Super-Precision } \\ \text { ( SP ) } \end{array}$ | Ultra-Precision ( UP) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Tolerance of height ( H ) | $\pm 0.1$ | $\pm 0.04$ | $\begin{gathered} 0 \\ -0.04 \end{gathered}$ | $\begin{gathered} 0 \\ -0.02 \end{gathered}$ | $\begin{gathered} 0 \\ -0.01 \end{gathered}$ |
| Tolerance of width ( W ) | $\pm 0.1$ | $\pm 0.04$ | $\begin{gathered} \hline 0 \\ -0.04 \end{gathered}$ | $\begin{gathered} \hline 0 \\ -0.02 \end{gathered}$ | $\begin{gathered} \hline 0 \\ -0.01 \end{gathered}$ |
| Difference of heights ( $\Delta \mathbf{H}$ ) | 0.03 | 0.02 | 0.01 | 0.005 | 0.003 |
| Difference of widths ( $\Delta \mathbf{W}$ ) | 0.03 | 0.02 | 0.01 | 0.005 | 0.003 |
| Running parallelism of BR Blocksurface $\mathbf{C}$ with respect to surface $\mathbf{A}$ | $\triangle$ C Refer to Fig.4-1 |  |  |  |  |
| Running parallelism of BR Block surface D with respect to surface | $\triangle$ D Refer to Fig.4-1 |  |  |  |  |



Fig. 4-1 BR rail length and running parallelism

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## Preload grade

| ITEM |  |  |
| :---: | :---: | :---: |
| GRADE $:$ Basic dynamic load rating |  |  |
| Clearance | Symbol | Preload force |
| No Preload | ZF | 0 |
| Light Preload | Z 1 | 0 |
| Middle Preload | Z 2 | 0.02 C |
| Heavy Preload | Z 3 | 0.05 C |

## Radial clearances

Unit: um

| Type $\mathbf{S y m b o l}$ | $\mathbf{Z F}$ | $\mathbf{Z 0}$ | $\mathbf{Z 1}$ | $\mathbf{Z 2}$ | $\mathbf{Z 3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{B R ~ 1 5}$ | $4 \sim 14$ | $-4 \sim 4$ | $-12 \sim-4$ | $-20 \sim-12$ | $-28 \sim-20$ |
| BR 20 | $5 \sim 15$ | $-5 \sim 5$ | $-14 \sim-5$ | $-23 \sim-14$ | $-32 \sim-23$ |
| BR $\mathbf{2 5}$ | $6 \sim 16$ | $-6 \sim 6$ | $-16 \sim-6$ | $-26 \sim-16$ | $-36 \sim-26$ |
| BR 30 | $7 \sim 17$ | $-7 \sim 7$ | $-19 \sim-7$ | $-31 \sim-19$ | $-43 \sim-31$ |
| BR 35 | $8 \sim 18$ | $-8 \sim 8$ | $-22 \sim-8$ | $-35 \sim-22$ | $-48 \sim-35$ |
| BR $\mathbf{4 5}$ | $10 \sim 20$ | $-10 \sim 10$ | $-25 \sim-10$ | $-40 \sim-25$ | $-55 \sim-40$ |
| BR $\mathbf{5 5}$ | $12 \sim 22$ | $-12 \sim 12$ | $-29 \sim-12$ | $-46 \sim-29$ | $-63 \sim-46$ |

## Rigidity of ABBA Linear Ball Rail with $\mathbf{Z} 2$ preload

Unit : kgf/um

| Type |  | Rigidity | Type |
| :---: | :---: | :---: | :---: |
| BR 20 | 50 | BR 35 | 80 |
| BR 25 | 58 | BR 45 | 125 |
| BR 30 | 66 | BR 55 | 190 |

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## Interchangeable and Non-interchangeable

|  | Non-interchangeable |  |  |  |  | Interchangeable |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Accuracy | UP | $\mathbf{S P}$ | $\mathbf{P}$ | $\mathbf{H}$ | $\mathbf{N}$ | $\mathbf{H}$ | $\mathbf{N}$ |
| Preload |  |  | Z 0 | Z 0 | Z 0 |  | ZF |
|  | Z 1 | Z 1 | Z 1 | Z 1 | Z 1 | Z 0 | Z 0 |
|  | Z 2 | Z 2 | Z 2 | Z 2 | Z 2 | Z 1 | Z 1 |
|  | Z 3 | Z 3 | Z 3 | Z 3 | Z 3 |  |  |

Suggestion in Assembly for ABBA Linear Ball Rail
Grinding Surface


Ra

imum Fillet

| ITEM | Maximum Fillet <br> (Ra) | Maximum Height (Hr) rail shoulder | Maximum Height (Hs) block shoulder | Rail Bolt Length (Lb) suggestion |
| :---: | :---: | :---: | :---: | :---: |
| BR 15 | 0.8 | 4 | 5 | M4*16 |
| BR 20 | 0.8 | 4.5 | 6 | M5*20 |
| BR 25 | 1.2 | 6 | 7 | M6*25 |
| BR 30 | 1.2 | 8 | 8 | M8*30 |
| BR 35 | 1.2 | 8.5 | 9 | M8*30 |
| BR 45 | 1.6 | 12 | 11 | M12*40 |
| BR 55 | 1.6 | 13 | 12 | M14*45 |

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## Permissible tolerances of mounting surfaces



Unit: um

| ITEM | Permissible tolerances for parallelism (e1 $)$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{Z 3}$ | $\mathbf{Z 2}$ | $\mathbf{Z 1}$ | $\mathbf{Z 0}$ | $\mathbf{Z F}$ | $\mathbf{Z 3}$ | $\mathbf{Z 2}$ | $\mathbf{Z 1}$ | $\mathbf{Z 0}$ | $\mathbf{Z F}$ |
| BR 15 |  |  | 18 | 25 | 35 |  |  | 85 | 130 | 190 |
| BR 20 |  | 18 | 20 | 25 | 35 |  | 50 | 85 | 130 | 190 |
| BR 25 | 15 | 20 | 22 | 30 | 42 | 60 | 70 | 85 | 130 | 195 |
| BR 30 | 20 | 27 | 30 | 40 | 55 | 80 | 90 | 110 | 170 | 250 |
| BR 35 | 22 | 30 | 35 | 50 | 68 | 100 | 120 | 150 | 210 | 290 |
| BR 45 | 25 | 35 | 40 | 60 | 85 | 110 | 140 | 170 | 250 | 350 |
| BR 55 | 30 | 45 | 50 | 70 | 95 | 125 | 170 | 210 | 300 | 420 |

## Tightening torque of screw

## Definition of Load and Life

## Basic static load rating: C0

When a linear motion system in the static state or in motion is subject to an extreme load or impact, a permanent deformation will occur between raceway and rolling elements. If the deformation is excessive, the linear motion system can not travel smoothly.

Now, we define the basic static load rating C 0 is a static load of constant magnitude acting in one direction under which the sum of the permanent deformations of rolling elements and raceway equals 0.0001 times the diameter of the rolling elements.

## Static permissible moment: M0

When a linear motion system is subject to a moment load, the maximum stress occurs in the rolling elements at both ends. The static permissible moment M0 is a moment of constant magnitude acting in one direction under which the sum of the permanent deformations of rolling elements and raceway equals 0.0001 times the diameter of the rolling elements.

## Basic static permissible moment: Mx , My, Mz

In the linear motion system, we define basic static permissible moments $\mathrm{Mx}, \mathrm{My}$ and Mz are the moments of the static permissible moment M 0 in $\mathrm{X}, \mathrm{Y}$ and Z direction.


## Static safety factor: fs

Static safety factor fs is the ratio of the basic static load rating C 0 to the load acting on the linear motion system.

$$
\mathrm{fs}=(\mathrm{fc} * \mathbf{C 0}) / \mathrm{P} \quad \text { or } \quad \mathrm{fs}=(\mathrm{fc} * \mathrm{M} 0) / \mathrm{M}
$$

fs : static safety factor
C 0 : basic static load rating
fc : Contact factor

P : design load
M0 : static permissible moment
M : design moment
Reference value of static safety factor fs shown below :

| Operating condition | Load condition | Minimum fs |
| :---: | :---: | :---: |
| Normally stationary | Small impact and deflection | $1.0 \sim 1.3$ |
|  | Impact or twisting load are applied | $2.0 \sim 3.0$ |
| Normally moving | Small impact or twisting load are applied | $1.0 \sim 1.5$ |
|  | Impact or twisting load are applied | $2.5 \sim 5.0$ |

## Nominal life: L

The nominal life L is the total distance of travel reached without flaking by $90 \%$ of a group of identical

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linear motion system that are operated independently under the same condition.

## Basic dynamic load rating: C

When each of a group of identical linear motion system is applied independently under the same condition, basic dynamic load rating C is the load of constant magnitude acting in one direction that results in a nominal life of 50 km for a system using balls.

## Contact factor: fc

In linear motion system, it is hard to obtain uniform load distribution in close contact installation due to moments, errors on the mounting surfaces and other factors. When two or more blocks in a rail are used in close contact, multiply basic load ratings C and C 0 by the contact factors shown below.

| Number of blocks in close contact | Contact factor |
| :---: | :---: |
| $\mathbf{2}$ | 0.81 |
| $\mathbf{3}$ | 0.72 |
| $\mathbf{4}$ | 0.66 |
| $\mathbf{5}$ | 0.61 |
| Normal operation | 1 |

## Formula of nominal life $\mathbf{L}$

Given the basic dynamic load rating $C$ and applied load $P$, the following formulas express the nominal life L of a linear motion system using balls.

$$
\mathrm{L}=\left(\frac{\mathrm{fh} * \mathrm{fT}^{* \mathrm{fc}}}{\mathrm{fw}} \mathrm{X} \frac{\mathrm{C}}{\mathrm{P}}\right)^{3} \mathrm{X} 50
$$

L: nominal life
C : basic dynamic load rating
P : applied load
fh : Hardness factor
fT : Temperature factor
fc : Contact factor
fw : Load factor

[^0]
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For linear motion system, its optimum load carrying capability is HrC 58 to 64 hardness on the raceways.
If the hardness is lower than HrC 58 , both the basic dynamic load rating and basic static load rating should be multiplied by hardness factor fh .


## Temperature factor: $\mathbf{f T}$

When a linear motion system is subject to temperature above $100^{\circ} \mathrm{C}$, the temperature factor should be taken into consideration.


Note 1: When used in above $80^{\circ} \mathrm{C}$, the seals and end plates should be designed for high temperature operation.

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Note 2: When used in above $120^{\circ} \mathrm{C}$, special treatment should be designed for stabilizing the dimension.

## Load factor: fw

Reciprocating motion usually occur vibrations, impacts and variable loads. In general, vibrations occur in high-speed operation, impacts due to repeated starting and stopping and variable loads it is difficult to calculate. When above factor affect the loading conditions significantly, divided basic load ratings C and C 0 by the experimentally obtained load factors shown below.

| Impacts and vibrations | Speed (V) | Measured vibration ( G ) | fw |
| :---: | :---: | :---: | :---: |
| Without external <br> Impacts <br> or Vibrations | At low speed <br> $\mathrm{V}<=15 \mathrm{~m} / \mathrm{min}$ | $\mathrm{G}<=0.5$ | $1 \sim 1.5$ |
| Without significant <br> Impacts <br> or Vibrations | At medium speed <br> $15<\mathrm{V}<=60 \mathrm{~m} / \mathrm{min}$ | $0.5<\mathrm{G}<=1.0$ | $1.5 \sim 2.0$ |
| With external <br> Impacts <br> or Vibrations | At high speed <br> $\mathrm{V}>60 \mathrm{~m} / \mathrm{min}$ | $1.0<\mathrm{G}<=2.0$ | $2.0 \sim 3.5$ |

## Frictional resistance

The frictional resistance can be calculated from following formula.

$$
\mathrm{F}=\mathrm{u} * \mathrm{~W}+\mathrm{f}
$$

F : frictional resistance
W : load
u : coefficient of friction
f : seal resistance

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Coefficient of friction : u


Seal resistance : f
Unit : kgf

| Model No. | resistance | Model No. | resistance |
| :---: | :---: | :---: | :---: |
| BR 15 | 0.3 | BR 35 | 0.7 |
| BR 20 | 0.4 | BR 45 | 0.9 |
| BR 25 | 0.4 | BR 55 | 1.0 |
| BR 30 | 0.5 |  |  |

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Mounting orientations

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## Fixing methods



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## Mounting procedure

```
set screw
```



Step 1 : Remove dents, burrs and dirt on mounting surfaces.
Step 2 : Place rail against the shoulder of mounting surfaces.
Step 3 : Tighten the mounting bolts lightly.
Note : i. check that holes on rail are aligned with the screw holes on mounting surfaces.
ii . do not tighten a bolt if the holes are not aligned.
Step 4 : Tighten the rail set screws.
Note : i . when tightening the mounting bolts, start with the bolt at the longitudinal center of the rail and move towards both rail ends.
Step 5 : Mount the other rail in the same way.
Step 6 : Install caps in mounting holes.
Step 7 : Place the table on the blocks carefully.
Step 8 : Tightening the block set screw to position the table.
Step 9 : Tighten the mounting bolts on the master and subsidiary blocks.
Note : i. Tighten the mounting bolts in the diagonal sequence.

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## Calculate the applied loads



$$
\begin{aligned}
& \text { Rn }=-\mathrm{Fz} / 4+\left(\mathrm{Fz}^{*}\right. \text { Pfy-Fy*Pfz)/(2*L1)-(Fx*Pfz-Fz*Pfx)/(2*L0) } \\
& \text { Rn }=-\mathrm{Fz} / 4+\left(\mathrm{Fz}^{*}\right. \text { Pfy-Fy*Pfz)/(2*L1)+(Fx*Pfz-Fz*Pfx)/(2*L0) } \\
& \text { Rn }=-\mathrm{Fz} / 4-\left(\mathrm{Fz}^{*}\right. \text { Pfy-Fy*Pfz)/(2*L1)+(Fx*Pfz-Fz*Pfx)/(2*L0) } \\
& \text { Rn }=-\mathrm{Fz} / 4-\left(\mathrm{Fz}^{*}\right. \text { Pfy-Fy*Pfz)/(2*L1)-(Fx*Pfz-Fz*Pfx)/(2*L0) } \\
& \text { Sc }=\mathrm{Fy} / 4+(\mathrm{Fy} * \text { Pfx-Fx*Pfy) } /(2 * \mathrm{~L} 0) \quad \mathrm{S} 2=\mathrm{Fy} / 4-(\mathrm{Fy} * \text { Pfx-Fx*Pfy)/(2*L0) } \\
& \text { Sc }=\text { Fy/4-(Fy*Pfx-Fx*Pfy)/(2*L0) S4=Fy/4+(Fy*Pfx-Fx*Pfy)/(2*L0) } \\
& \nabla \mathrm{X}=(\mathrm{R} 2-\mathrm{R} 1) *(\mathbf{P f z}) /(\mathrm{L} 0 * \mathrm{Kr})+(\mathbf{S 2} 2 \mathbf{S} 1) *(\mathrm{Pfy}) /(\mathrm{L0} 0 \text { Ks }) \\
& \nabla \mathrm{Y}=(\mathrm{R} 2-\mathrm{R} 3) *(\mathrm{Pfz}) /(\mathrm{L} 1 * \mathrm{Kr})+(\mathrm{S} 2-\mathrm{S} 1) *(\mathrm{Pfx}) /(\mathrm{L} 0 * \mathrm{Ks})-(\mathrm{S} 2+\mathrm{S} 1) /(2 * \mathrm{Ks}) \\
& \nabla \mathrm{Z}=(\mathrm{R} 2+\mathrm{R} 4) /(2 * \mathrm{Kr})+(\mathrm{R} 1-\mathrm{R} 2) *(\mathbf{P f x}) /(\mathrm{L} 0 * \mathbf{P f y}) /(\mathrm{L} 1 * \mathrm{Kr})
\end{aligned}
$$

User input data :
Fr : Load in X direction ( - or + ) kg $\quad$ Fy : Load in Y direction ( - or + ) kgf

Fz : Load in $\mathbf{Z}$ direction ( - or + ) kgf
Pay: Position in Y direction (-or + ) mm
L0 : Distance in blocks ( mm )

Pix : Position in $\mathbf{X}$ direction ( - or + ) mm
Pf : Positon in $\mathbf{Z}$ direction ( - or + ) mm
L1 : Distance in rails ( mm )

The applied loads for BR Linear Motion System (kgf) :
R1 : Radial load for Block Now. ( - or + )
R2: Radial load for Block No. ( - or + )

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R3 : Radial load for Block No3. ( - or + )
S1 : Lateral load for Block No1. ( - or + )
S3 : Lateral load for Block No3. ( - or + )
Deformation ( mm ) for applied loads :
Kr : Stiffness in Radial direction ( kgf/um )
$\nabla$ X: Deflection in X direction ( $-\mathrm{or}+$ ) mm
$\nabla \mathrm{Z}$ : Deflection in $\mathbf{Z}$ direction ( $-\mathrm{or}+$ ) mm

R4 : Radial load for Block No4. ( - or + )
S2 : Lateral load for Block No2. ( - or + )
S4 : Lateral load for Block No4. ( - or + )

Ks : Stiffness in Lateral direction ( kgf/um )
$\nabla \mathrm{Y}:$ Deflection in Y direction ( - or + ) mm

## Example 1 :



This case is divided into three sections.
Section 1 : it is subject to

(W/g)*A(acceleration) ------- Fx(A)
Section 2 : we are subject to

$$
\Rightarrow \text { W(weight) ---------------------- Fx(W) }
$$

Section 3 : we are subject to

$$
\begin{aligned}
& \Rightarrow W(\text { weight }) \text { and } \\
& \text { Fx(W) }
\end{aligned}
$$

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(W/g)*(-A)(deceleration) ---- Fx(-A)

## User input data :

$$
\begin{array}{lrl}
V * V=V 0 * V 0+2 * A * D 1 \Rightarrow & A=(V * V-V 0 * V 0) /(2 * D 1) \\
D 1=1000 ~ m m ~ & & D 2=2000 \mathrm{~mm}
\end{array}
$$

$$
\begin{array}{lllll}
V=1 \mathrm{~m} / \mathrm{s} & \mathrm{~V} 0=0 \mathrm{~m} / \mathrm{s} & \Rightarrow & (\mathrm{~A})=0.5 \mathrm{~m} / \mathrm{s}^{2} & \text { for acceleration } \\
\mathrm{V}=0 \mathrm{~m} / \mathrm{s} & \mathrm{~V} 0=1 \mathrm{~m} / \mathrm{s} & \Rightarrow & (-\mathrm{A})=-0.5 \mathrm{~m} / \mathrm{s}^{2} & \text { for deceleration }
\end{array}
$$

| $F x(W)=98 \mathrm{kgf}$ | $F y(W)=0$ | $F z(W)=0$ |
| :--- | :--- | :--- |
| $F x(A)=(98 / 9.8) * 0.5=5 \mathrm{kgf}$ | $F y(A)=0$ | $F z(A)=0$ |
| $F x(-A)=(98 / 9.8) *(-0.5)=-5 \mathrm{kgf}$ | $F y(-A)=0$ | $F z(-A)=0$ |

$\mathbf{P f x}=\mathbf{8 0} \mathrm{mm}$
$\mathrm{L} 0=\mathbf{3 0 0} \mathrm{mm}$

Pfy $=\mathbf{2 5 0} \mathbf{~ m m}$
Pfz $=280 \mathrm{~mm}$
$\mathrm{L} 1=\mathbf{5 0 0} \mathbf{~ m m}$
$\mathrm{f} \mathbf{w}=\mathbf{1 . 5}$

## Calculation applied loads :

R1 $(W)=-F x(W) * P f z /(2 * L 0)=-45.73 \mathrm{kgf}$
R2 $(W)=F x(W) * P f z /(2 * L 0)=45.73 \mathrm{kgf}$
$R 3(W)=F x(W) * P f z /(2 * L 0)=45.73 \mathrm{kgf}$
$R 4(W)=-F x(W) * P f z /(2 * L 0)=-45.73 \mathrm{kgf}$
$R 1(A)=-F x(A) * P f z /(2 * L 0)=-2.33 \mathrm{kgf}$
$\mathrm{R} 2(\mathrm{~A})=\mathrm{Fx}(\mathrm{A}) * \mathrm{Pfz} /(2 * \mathrm{~L} 0)=2.33 \mathrm{kgf}$
$R 3(A)=F x(A) * P f z /(2 * L 0)=2.33 \mathrm{kgf}$
$R 4(A)=-\mathrm{Fx}(A) * \mathrm{Pfz} /(2 * \mathrm{~L} 0)=-2.33 \mathrm{kgf}$
$\mathrm{R} 1(-\mathrm{A})=-\mathrm{Fx}(-\mathrm{A}) * \mathrm{Pfz} /(2 * \mathrm{~L} 0)=2.33 \mathrm{kgf}$
R2(-A) $=\mathbf{F x}(-\mathrm{A}) * \mathbf{P f z} /(2 * \mathrm{~L} 0)=\mathbf{- 2 . 3 3} \mathbf{~ k g f}$
R3 $(-\mathrm{A})=\mathrm{Fx}(-\mathrm{A}) * \mathrm{Pfz} /(2 * \mathrm{~L} 0)=-\mathbf{2 . 3 3} \mathbf{~ k g f}$
$\mathrm{R} 4(-\mathrm{A})=-\mathrm{Fx}(-\mathrm{A}) * \mathrm{Pfz} /(2 * \mathrm{~L} 0)=2.33 \mathrm{kgf}$
S1 $(W)=-F x(W) * P f y /(2 * L 0)=-40.83 \mathrm{kgf}$
$\mathrm{S} 2(\mathrm{~W})=\mathrm{Fx}(\mathrm{W}) * \mathrm{Pfy} /(2 * \mathrm{~L} 0)=40.83 \mathrm{kgf}$
$\mathrm{S} 3(\mathrm{~W})=\mathrm{Fx}(\mathrm{W}) * \mathrm{Pfy} /(2 * \mathrm{~L} 0)=40.83 \mathrm{kgf}$
$S 4(W)=-F x(W) * P f y /(2 * L 0)=-40.83 \mathrm{kgf}$
$S 1(A)=-F x(A) * P f y /(2 * L 0)=-2.08 \mathrm{kgf}$
$\mathrm{S} 2(\mathrm{~A})=\mathrm{Fx}(\mathrm{A}) * \mathrm{Pfy} /(2 * \mathrm{~L} 0)=\mathbf{2 . 0 8} \mathrm{kgf}$
$\mathrm{S} 3(\mathrm{~A})=\mathrm{Fx}(\mathrm{A}) * \mathrm{Pfy} /(2 * \mathrm{~L} 0)=2.08 \mathrm{kgf}$
$\mathrm{S} 4(\mathrm{~A})=-\mathrm{Fx}(\mathrm{A}) * \mathrm{Pfy} /(2 * \mathrm{~L} 0)=-2.08 \mathrm{kgf}$
S1 (-A) $=-\mathrm{Fx}(-\mathrm{A}) * \mathrm{Pfy} /(2 * \mathrm{~L} 0)=2.08 \mathrm{kgf}$
S2(-A) $=\mathrm{Fx}(-\mathrm{A}) * \mathrm{Pfy} /(2 * \mathrm{~L} 0)=-2.08 \mathrm{kgf}$
S3(-A) $=\mathbf{F x}(-\mathrm{A}) * \mathrm{Pfy} /(2 * \mathrm{~L} 0)=-2.08 \mathrm{kgf}$
S4(-A) $=-\mathrm{Fx}(-\mathrm{A}) * \mathrm{Pfy} /(2 * \mathrm{~L} 0)=2.08 \mathrm{kgf}$

The applied load - section 1 :

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$R 1(1)=R 1(W)+R 1(A)=-48.06 \mathrm{kgf}$
R2(1) $=$ R2 $(\mathrm{W})+\mathrm{R} 2(\mathrm{~A})=48.06 \mathrm{kgf}$
R3(1) $=$ R3 $(\mathrm{W})+\mathrm{R} 3(\mathrm{~A})=48.06 \mathrm{kgf}$
R4 $(1)=$ R4 $(\mathrm{W})+\mathrm{R} 1(\mathrm{~A})=-48.06 \mathrm{kgf}$

The applied load - section 2 :

$$
R 1(2)=R 1(W)=-45.73 \mathrm{kgf}
$$

R2(2) $=\mathbf{R} 2(W)=45.73 \mathrm{kgf}$
R3(2) $=$ R3 $(\mathrm{W})=45.73 \mathrm{kgf}$
$R 4(2)=R 4(W)=-45.73 \mathbf{~ k g f}$

The applied load - section 3 :
R1 $(3)=R 1(W)+R 1(-A)=-43.4 \mathrm{kgf}$
R2(3) = R2(W)+R2(-A) = 43.4 kgf
R3(3) $=$ R3 $(\mathrm{W})+\mathrm{R} 3(-\mathrm{A})=43.4 \mathrm{kgf}$
$R 4(3)=R 4(W)+R 1(-A)=-43.4 \mathrm{kgf}$

S1 $(1)=\mathrm{S} 1(\mathrm{~W})+\mathrm{S} 1(\mathrm{~A})=-42.91 \mathrm{kgf}$
S2(1) $=\mathbf{S} 2(W)+$ S2 $(A)=42.91 \mathrm{kgf}$
S3(1) $=$ S3 $(W)+$ S3 $(A)=42.91 \mathrm{kgf}$
S4(1) $=\mathbf{S 4}(\mathrm{W})+\mathrm{S} 4(\mathrm{~A})=-42.91 \mathrm{kgf}$
$S 1(2)=S 1(W)=-40.83 \mathbf{~ k g f}$
S2(2) $=$ S2 $(W)=40.83 \mathrm{kgf}$
S3(2) $=\mathrm{S} 3(\mathrm{~W})=40.83 \mathrm{kgf}$
$S 4(2)=S 4(W)=-40.83 \mathbf{~ k g f}$

S1 (3) $=\mathbf{S 1}(\mathrm{W})+\mathrm{S} 1(-\mathrm{A})=-38.75 \mathrm{kgf}$
S2(3) = S2(W) + S2 (-A) $=38.75 \mathrm{kgf}$
S3(3) $=\mathbf{S 3}(\mathrm{W})+$ S3 (-A $)=38.75 \mathrm{kgf}$
S4 $(3)=\mathrm{S} 4(\mathrm{~W})+\mathrm{S} 4(-\mathrm{A})=-38.75 \mathrm{kgf}$

## Calculate the single equivalent load

When a radial load ( Rn ) and lateral load ( Sn ) are exerted simultaneously,the single equivalent load is expressed by the following equation for $B R$ linear motion system.

$$
\mathbf{R e}=\mathbf{R n}+\mathbf{S n}
$$

The single equivalent load - section $1: \mathbf{R 1 1 , R 2 1 , R 3 1 ~ \& ~ R 4 1 ~}$

$$
\begin{array}{ll}
\mathbf{R} 11=|\mathrm{R} 1(1)|+|\mathrm{S} 1(1)|=90.97 \mathrm{kgf} & \mathrm{R} 21=|\mathrm{R} 2(1)|+|\mathrm{S} 2(1)|=90.97 \mathrm{kgf} \\
\mathrm{R} 31=|\mathrm{R} 3(1)|+|\mathrm{S} 3(1)|=90.97 \mathrm{kgf} & \\
\text { R41 } & =|\mathrm{R} 4(1)|+|\mathrm{S} 4(1)|=90.97 \mathrm{kgf}
\end{array}
$$

The single equivalent load - section 2 : R12,R22,R32 \& R42

$$
\begin{array}{ll}
\mathrm{R} 12=|\mathrm{R} 1(2)|+|\mathrm{S} 1(2)|=86.56 \mathrm{kgf} & \mathrm{R} 22=|\mathrm{R} 2(2)|+|\mathrm{S} 2(2)|=86.56 \mathrm{kgf} \\
\mathrm{R} 32=|\mathrm{R} 3(2)|+|\mathrm{S} 3(2)|=86.56 \mathrm{kgf} & \mathrm{R} 42=|\mathrm{R} 4(2)|+|\mathrm{S} 4(2)|=86.56 \mathrm{kgf}
\end{array}
$$

The single equivalent load - section 3 : R13,R23,R33 \& R43

$$
\begin{array}{ll}
\mathbf{R 1 3}=|\mathbf{R 1}(3)|+|\mathrm{S} 1(3)|=82.15 \mathrm{kgf} & \mathrm{R} 23=|\mathrm{R} 2(3)|+|\mathrm{S} 2(3)|=82.15 \mathrm{kgf} \\
\mathrm{R} 33=|\mathrm{R} 3(3)|+|\mathrm{S} 3(3)|=82.15 \mathrm{kgf} & \mathrm{R} 43=|\mathrm{R} 4(3)|+|\mathrm{S} 4(3)|=82.15 \mathrm{kgf}
\end{array}
$$

## (A)ABBA Linear Ball Rail ---- $B R$ series

## International Standard Dimension Design

## Calculate the mean load

We must calculate the mean value of the varying load to evaluate the life of BR linear motion system.

## Step loads

$$
P m=\left[\left(P 1^{n} \times L 1+P 2^{n} \times L 2 \ldots . .+P n^{n} \times L n\right) / L\right]^{1 / n}
$$

Pm : Mean load ( kgf)
Pn : Varying load ( kgf)
$L$ : Total length of travel ( mm )
Ln : Length of travel carrying Pn ( mm )
$\mathrm{n}=\mathbf{3}$ when the rolling elements are balls.


## Loads that vary linearly

Pm= $(\mathbf{P m i n}+2 x P m a x) / 3$

Pmim : Minimum load (kgf)
Pmax : Maximum load (kgf)


## Loads varying sinusoidally




Now we calculate the mean loads of example 1. ( step load type ) : R1,R2,R3 \& R4
(A)ABBA Linear Ball Rail ---- $B R$ series

## International Standard Dimension Design

$$
\begin{aligned}
& R 1=\left[\left(R 11^{3} \times 1000+R 12^{3} \times 2000+R 13^{3} \times 1000\right) / 4000\right]^{1 / 3}=86.7 \mathrm{kgf} \\
& R 2=\left[\left(R 21^{3} \times 1000+R 22^{3} \times 2000+R 23^{3} \times 1000\right) / 4000\right]^{1 / 3}=86.7 \mathrm{kgf} \\
& R 3=\left[\left(R 31^{3} \times 1000+R 32^{3} \times 2000+R 33^{3} \times 1000\right) / 4000\right]^{1 / 3}=86.7 \mathrm{kgf} \\
& R 4=\left[\left(R 41^{3} \times 1000+R 42^{3} \times 2000+\text { R43 }^{3} \times 1000\right) / 4000\right]^{1 / 3}=86.7 \mathbf{~ k g f}
\end{aligned}
$$

## Calculate nominal life L

$$
L=\left(\frac{f h * f T^{*} f c}{f w} \times \frac{C}{P}\right)^{3} \times 50 \quad \mathrm{~km}
$$

$B R$ linear motion system of use : BRH20A $2 \mathrm{~L} 4000 \mathrm{NZ0}=>\mathrm{C}=1450 \mathrm{kgf} \quad \mathrm{C} 0=\mathbf{2 5 6 0} \mathbf{~ k g f}$ Given: ( $\mathbf{P}$ : the mean load )

$$
\begin{array}{lcrr}
\mathrm{fh}=\mathbf{1} & \mathrm{fT}=1 & \mathrm{fc}=1 & \& \\
\mathrm{~L} 1=[\mathrm{C} /(\mathrm{R} 1 \mathrm{xfw})]^{3} \times 50=69351.5 \mathrm{~km} & \mathrm{~L} 2=[\mathrm{C} /(\mathrm{R} 2 \times f \mathrm{f})]^{3} \times 50=69351.5 \mathrm{~km} \\
\mathrm{~L} 3=[\mathrm{C} /(\mathrm{R} 3 \times f \mathrm{xw})]^{3} \times 50=69351.5 \mathrm{~km} & \mathrm{~L} 4=[\mathrm{C} /(\mathrm{R} 4 \times f \mathrm{f})]^{3} \times 50=69351.5 \mathrm{~km}
\end{array}
$$

## calculate static safety factor fs

$$
\mathrm{fs}=(\mathrm{fc} * \mathbf{C 0}) / \mathrm{P}=\mathbf{2 5 6 0} / \mathrm{R} 11=28.14
$$

( $\mathrm{P}:$ : Maximum single equivalent load $=$ R11 or R21 or R31 or R41 )


[^0]:    Hardness factor: fh

